

CHITKARA UNIVERSITY, HIMACHAL PRADESH

DECLARATION BY THE STUDENT

I **Jai Chand** (PHDASM19063) hereby certify that the work which is being presented in this thesis entitled “**Analysis of Vibrations of Electro-Magneto Transversely Isotropic Thermoelastic Materials with Voids**” is for the fulfillment of the requirement for the award of Degree of **Doctor of Philosophy** submitted in the **Department of Applied Sciences (Mathematics), Chitkara University, Himachal Pradesh** is an authentic record of my own work carried out under the supervision of **Dr Sita Ram**.

The work has not formed the basis for the award of any other degree or diploma, in this or any other Institution or University. In keeping with the ethical practice in reporting scientific information, due acknowledgements have been made wherever the findings of others have been cited.

Jai Chand

CERTIFICATE BY THE SUPERVISOR

This is to certify that the thesis entitled “**Analysis of Vibrations of Electro-Magneto Transversely Isotropic Thermoelastic Materials with Voids**” submitted by Mr Jai Chand with Regd. No. PHDASM19063 to the Chitkara University, Himachal Pradesh in fulfillment for the award of the degree of Doctor of Philosophy is a bonafide record of research work carried out by him under my supervision. The contents of this thesis, in full or in parts, have not been submitted to any other Institution or University for the award of any degree or diploma.

Dr. Sita Ram

Professor, Department of Applied Sciences,
Chitkara University, Himachal Pradesh

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DEDICATED

TO

MEHALWAL FAMILY

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